

```
<!DOCTYPE html>

<html lang="zh-CN">

<head>

  <meta charset="UTF-8">

  <meta name="viewport" content="width=device-width, initial-scale=1.0">

  <title>静载荷 vs 突加载荷 · 动荷系数演示</title>

  <style>

    * {

      margin: 0;

      padding: 0;

      box-sizing: border-box;

    }

    body {

      font-family: 'Segoe UI', 'PingFang SC', Roboto, sans-serif;

      background: #eef2f7;

      display: flex;

      justify-content: center;

      padding: 16px 12px;

      min-height: 100vh;

    }

    .container {

      max-width: 1000px;

      width: 100%;

      background: #ffffff;

      border-radius: 24px;
```

```
    box-shadow: 0 12px 40px rgba(0, 0, 0, 0.10);  
    padding: 20px 24px 28px;  
    transition: 0.2s;  
}
```

```
h1 {  
    font-weight: 600;  
    font-size: 26px;  
    color: #1f2b38;  
    display: flex;  
    align-items: center;  
    gap: 10px;  
    flex-wrap: wrap;  
    margin-bottom: 2px;  
}
```

```
h1 small {  
    font-size: 15px;  
    font-weight: 400;  
    color: #6b7f93;  
    margin-left: 4px;  
}
```

```
.subhead {  
    color: #6b7f93;  
    font-size: 14px;  
    border-bottom: 2px solid #edf2f7;  
    padding-bottom: 12px;
```

```
margin-bottom: 14px;

display: flex;

justify-content: space-between;

flex-wrap: wrap;

gap: 6px 14px;
}
```

```
.subhead .badge {

background: #eaf0f8;

padding: 2px 14px;

border-radius: 20px;

font-weight: 500;

color: #1f2b38;

font-size: 13px;
}
```

```
/* 画布 */
```

```
.canvas-wrap {

background: #f9fbfd;

border-radius: 16px;

border: 1px solid #e4ebf3;

overflow: hidden;

position: relative;

margin-bottom: 14px;

text-align: center;
}
```

```
.canvas-wrap canvas {

display: block;
```

```
        width: 100%;  
        height: auto;  
        background: #fafcfe;  
        touch-action: none;  
    }  
}
```

```
/* 控制面板 */
```

```
.ctrl-panel {  
    background: #f7f9fc;  
    border-radius: 14px;  
    border: 1px solid #e4ebf3;  
    padding: 14px 18px 16px;  
    margin-bottom: 14px;  
    display: flex;  
    flex-wrap: wrap;  
    gap: 8px 20px;  
    align-items: center;  
    justify-content: center;  
}
```

```
.ctrl-item {  
    display: flex;  
    align-items: center;  
    gap: 6px 10px;  
    flex: 1 1 160px;  
    min-width: 120px;  
    max-width: 240px;  
}
```

```
.ctrl-item label {  
    font-size: 14px;  
    font-weight: 600;  
    color: #2c3e50;  
    white-space: nowrap;  
    min-width: 20px;  
}  
  
.ctrl-item label .sym {  
    font-style: italic;  
    font-weight: 700;  
}  
  
.ctrl-item input[type="range"] {  
    flex: 1;  
    min-width: 50px;  
    -webkit-appearance: none;  
    appearance: none;  
    height: 4px;  
    border-radius: 4px;  
    background: #d0d9e6;  
    outline: none;  
    transition: 0.2s;  
}  
  
.ctrl-item input[type="range"]::-webkit-slider-thumb {  
    -webkit-appearance: none;  
    width: 18px;  
    height: 18px;  
    border-radius: 50%;
```

```

        background: #2c3e50;

        border: 2px solid #fff;

        box-shadow: 0 2px 6px rgba(0, 0, 0, 0.18);

        cursor: pointer;

        transition: 0.15s;
    }

    .ctrl-item input[type="range"]::-webkit-slider-thumb:hover {

        transform: scale(1.12);
    }

    .ctrl-item input[type="range"]::-moz-range-thumb {

        width: 18px;

        height: 18px;

        border-radius: 50%;

        background: #2c3e50;

        border: 2px solid #fff;

        cursor: pointer;
    }

    .ctrl-item .val {

        font-weight: 600;

        font-size: 15px;

        min-width: 44px;

        text-align: right;

        font-variant-numeric: tabular-nums;

        color: #1a2634;
    }

    .ctrl-item .val .unit {

        font-weight: 400;

```

```
    font-size: 11px;

    color: #7f8c9e;

    margin-left: 1px;
}
```

```
.ctrl-item.color-p input[type="range"] {

    background: linear-gradient(to right, #fde8e8, #e74c3c);

}
```

```
.ctrl-item.color-k input[type="range"] {

    background: linear-gradient(to right, #e3f0fc, #2980b9);

}
```

```
.ctrl-item.color-z input[type="range"] {

    background: linear-gradient(to right, #e8f5e9, #27ae60);

}
```

```
.btn-group {

    display: flex;

    gap: 8px;

    flex-wrap: wrap;

    align-items: center;

}
```

```
.btn {

    padding: 8px 24px;

    border: none;

    border-radius: 10px;

    font-size: 14px;

    font-weight: 600;
```

```
        cursor: pointer;

        transition: 0.25s;

        background: #e6ecf5;

        color: #3d5066;
    }

    .btn:hover {

        background: #d5dee9;

        transform: translateY(-1px);
    }

    .btn-primary {

        background: #2c3e50;

        color: #fff;
    }

    .btn-primary:hover {

        background: #1a2634;
    }

    .btn-success {

        background: #27ae60;

        color: #fff;
    }

    .btn-success:hover {

        background: #1e8449;
    }

    .btn-danger {

        background: #e74c3c;

        color: #fff;
    }
```

```
.btn-danger:hover {  
    background: #c0392b;  
}  
  
.btn.active {  
    box-shadow: 0 0 0 3px rgba(44, 62, 80, 0.3);  
}
```

```
/* 信息区 */
```

```
.info-area {  
    display: flex;  
    flex-wrap: wrap;  
    gap: 6px 20px;  
    background: #f2f6fb;  
    border-radius: 12px;  
    padding: 10px 16px;  
    border: 1px solid #e4ebf3;  
    margin-bottom: 10px;  
    align-items: center;  
    justify-content: center;  
}
```

```
.info-item {  
    display: flex;  
    align-items: baseline;  
    gap: 4px 6px;  
    font-size: 14px;  
    color: #1f2b38;  
    flex-wrap: wrap;
```

```
}

.info-item .tag {
    font-weight: 400;
    color: #6b7f93;
}

.info-item .num {
    font-weight: 700;
    font-variant-numeric: tabular-nums;
}

.info-item .num.red {
    color: #c0392b;
}

.info-item .num.blue {
    color: #2980b9;
}

.info-item .num.green {
    color: #27ae60;
}

.info-item .num.purple {
    color: #8e44ad;
}

.info-item .num.orange {
    color: #d35400;
}

/* 公式区 */

.formula-box {
```

```
background: #fafcfe;

border-radius: 12px;

border: 1px solid #e4ebf3;

padding: 10px 16px;

font-size: 15px;

color: #1a2634;

display: flex;

flex-wrap: wrap;

align-items: center;

gap: 6px 18px;

min-height: 44px;
}

.formula-box .math {

    font-family: 'Cambria', 'Times New Roman', serif;

    font-style: italic;

    background: #eef4fa;

    padding: 2px 14px;

    border-radius: 8px;

    font-size: 16px;

    line-height: 1.8;
}

.formula-box .math .hl-red {

    color: #c0392b;

    font-weight: 700;
}

.formula-box .math .hl-blue {

    color: #2980b9;
```

```
        font-weight: 700;
    }

    .formula-box .math .hl-green {
        color: #27ae60;
        font-weight: 700;
    }

    .formula-box .math .hl-orange {
        color: #d35400;
        font-weight: 700;
    }

    .formula-box .math .hl-purple {
        color: #8e44ad;
        font-weight: 700;
    }

    .status-bar {
        display: flex;
        flex-wrap: wrap;
        gap: 8px 18px;
        padding: 4px 0 2px 0;
        font-size: 13px;
        color: #6b7f93;
        justify-content: center;
    }

    .status-bar .dot {
        display: inline-block;
        width: 10px;
```

```
        height: 10px;

        border-radius: 50%;

        margin-right: 4px;
    }

    .status-bar .dot.green {

        background: #27ae60;
    }

    .status-bar .dot.orange {

        background: #e67e22;
    }

    .status-bar .dot.red {

        background: #e74c3c;
    }

    .status-bar .dot.blue {

        background: #2980b9;
    }

    @media (max-width: 760px) {

        .container {

            padding: 12px 12px 18px;
        }

        .ctrl-panel {

            flex-direction: column;

            align-items: stretch;

            gap: 6px;
        }

        .ctrl-item {
```

```
        flex: 1 1 100%;

        max-width: 100%;
    }

    .btn-group {
        justify-content: center;
    }

    .info-area {
        flex-direction: column;
        align-items: stretch;
        gap: 3px;
    }

    .formula-box {
        flex-direction: column;
        align-items: flex-start;
        font-size: 14px;
    }

    .formula-box .math {
        font-size: 14px;
        padding: 2px 10px;
    }

    h1 {
        font-size: 20px;
    }

    h1 small {
        font-size: 13px;
    }
}
```

```

    @media (max-width: 480px) {
        .ctrl-item label {
            font-size: 13px;
            min-width: 18px;
        }
        .ctrl-item .val {
            font-size: 13px;
            min-width: 36px;
        }
        .btn {
            padding: 6px 14px;
            font-size: 13px;
        }
    }
</style>
</head>
<body>

<div class="container">
    <h1>

        ⚡ 静载荷 vs 突加载荷 · 动荷系数演示

        <small>突加载荷  $K_d \equiv 2$ </small>

    </h1>
    <div class="subhead">
        <span>对比静载与突加载荷的变形 · 动应力差异</span>

        <span class="badge"> $K_d = 1 + \sqrt{1 + 2h/\delta}$ </span>
    
```



```

        <span class="val" id="valK">8000<span
class="unit">N/m</span></span>

    </div>

    <div class="ctrl-item color-z">

        <label><span class="sym"> $\zeta$ </span></label>

        <input type="range" id="sliderZeta" min="0" max="0.30"
step="0.01" value="0.05">

        <span class="val" id="valZeta">0.05</span>

    </div>

    <div class="btn-group">

        <button class="btn btn-primary active" id="btnStatic">🏠 静载
</button>

        <button class="btn btn-danger" id="btnSudden">💥 突加载荷
</button>

        <button class="btn btn-success" id="btnReset">↺ 复位</button>

    </div>

</div>

<!-- 信息栏 -->

<div class="info-area" id="infoArea">

    <span class="info-item"><span class="tag">静变形</span>  $\delta$ 
<sub>st</sub> = <span class="num purple" id="infoDeltaSt">—</span></span>

    <span class="info-item"><span class="tag">静应力</span>  $\sigma$ 
<sub>st</sub> = <span class="num blue" id="infoSigmaSt">—</span></span>

    <span class="info-item"><span class="tag">最大动变形</span>  $\delta$ 
<sub>d</sub> = <span class="num orange" id="infoDeltaD">—</span></span>

    <span class="info-item"><span class="tag">最大动应力</span>  $\sigma$ 
<sub>d</sub> = <span class="num red" id="infoSigmaD">—</span></span>

```



```
canvas.width = W;
```

```
canvas.height = H;
```

```
const sliderP = document.getElementById('sliderP');
```

```
const sliderK = document.getElementById('sliderK');
```

```
const sliderZeta = document.getElementById('sliderZeta');
```

```
const valP = document.getElementById('valP');
```

```
const valK = document.getElementById('valK');
```

```
const valZeta = document.getElementById('valZeta');
```

```
const infoDeltaSt = document.getElementById('infoDeltaSt');
```

```
const infoSigmaSt = document.getElementById('infoSigmaSt');
```

```
const infoDeltaD = document.getElementById('infoDeltaD');
```

```
const infoSigmaD = document.getElementById('infoSigmaD');
```

```
const infoKd = document.getElementById('infoKd');
```

```
const formulaKdVal = document.getElementById('formulaKdVal');
```

```
const formulaSigmaVal = document.getElementById('formulaSigmaVal');
```

```
const modeStatus = document.getElementById('modeStatus');
```

```
const statusDetail = document.getElementById('statusDetail');
```

```
const btnStatic = document.getElementById('btnStatic');
```

```
const btnSudden = document.getElementById('btnSudden');
```

```
const btnReset = document.getElementById('btnReset');
```

```
// ----- 物理参数 -----
```

```
const g = 9.81;

const A = 1e-4; // 截面积 m² (固定)

let P = 400; // N

let k = 8000; // N/m

let zeta = 0.05; // 阻尼比


// 计算物理量

let deltaSt = 0; // 静变形

let sigmaSt = 0; // 静应力

let omega = 0; // 固有频率


// 动画状态

let mode = 'static'; // 'static' | 'sudden'

let time = 0;

let delta = 0; // 当前变形

let deltaMax = 0; // 最大变形 (用于显示)

let animId = null;

let isAnimating = false;

let resetRequested = false;


// 画布几何

const topY = 60;

const bottomY = 390;

const L0 = bottomY - topY; // 杆件原始长度 (px)

const cx = W / 2;

const scaleFactor = 280; // 变形缩放 (px/m)
```

```

// ----- 物理计算 -----

function computePhysics() {

    deltaSt = P / k;

    sigmaSt = P / A;

    const m = P / g;

    omega = Math.sqrt(k / m);

}


// ----- 更新显示数值 -----

function updateDisplay() {

    computePhysics();


    const deltaD = (mode === 'sudden') ? 2 * deltaSt : deltaSt;
    const sigmaD = (mode === 'sudden') ? 2 * sigmaSt : sigmaSt;
    const Kd = (mode === 'sudden') ? 2.0 : 1.0;


    infoDeltaSt.textContent = (deltaSt * 1000).toFixed(2) + ' mm';
    infoSigmaSt.textContent = (sigmaSt / 1e6).toFixed(2) + ' MPa';
    infoDeltaD.textContent = (deltaD * 1000).toFixed(2) + ' mm';
    infoSigmaD.textContent = (sigmaD / 1e6).toFixed(2) + ' MPa';
    infoKd.textContent = Kd.toFixed(3);


    formulaKdVal.textContent = Kd.toFixed(3);

    formulaSigmaVal.textContent = (sigmaD / 1e6).toFixed(2) + ' MPa';

}


// ----- 绘制场景 -----

```

```
function drawScene(currentDelta, maxDelta, phase) {  
    ctx.clearRect(0, 0, W, H);  
  
    // ---- 背景网格 ----  
    ctx.save();  
    ctx.strokeStyle = '#eef2f7';  
    ctx.lineWidth = 0.5;  
    for (let i = 0; i < 20; i++) {  
        const x = 20 + i * 40;  
        ctx.beginPath();  
        ctx.moveTo(x, 20);  
        ctx.lineTo(x, H - 20);  
        ctx.stroke();  
    }  
    for (let i = 0; i < 15; i++) {  
        const y = 20 + i * 32;  
        ctx.beginPath();  
        ctx.moveTo(20, y);  
        ctx.lineTo(W - 20, y);  
        ctx.stroke();  
    }  
    ctx.restore();  
  
    // ---- 固定端 ----  
    ctx.save();  
    ctx.fillStyle = '#34495e';  
    ctx.shadowColor = 'rgba(0,0,0,0.08)';
```

```
ctx.shadowBlur = 8;

ctx.fillRect(cx - 55, topY - 18, 110, 18);

ctx.shadowBlur = 0;

ctx.fillStyle = '#5d6d7e';

for (let i = -35; i <= 35; i += 18) {

    ctx.beginPath();

    ctx.arc(cx + i, topY - 9, 4, 0, 2 * Math.PI);

    ctx.fill();

}

ctx.fillStyle = '#2c3e50';

ctx.font = '13px "Segoe UI", sans-serif';

ctx.textAlign = 'center';

ctx.textBaseline = 'bottom';

ctx.fillText('固定端', cx, topY - 22);

ctx.restore();


// ---- 原始位置参考线 (虚线) ----

ctx.save();

ctx.setLineDash([5, 6]);

ctx.strokeStyle = 'rgba(44,62,80,0.25)';

ctx.lineWidth = 1.2;

ctx.beginPath();

ctx.moveTo(cx - 60, bottomY);

ctx.lineTo(cx + 60, bottomY);

ctx.stroke();

ctx.setLineDash([]);

ctx.fillStyle = 'rgba(44,62,80,0.3)';
```

```

    ctx.font = '11px "Segoe UI", sans-serif';

    ctx.textAlign = 'left';

    ctx.textBaseline = 'top';

    ctx.fillText('原始位置', cx + 64, bottomY - 6);

    ctx.restore();

    // ---- 杆件 ----

    const deformPx = currentDelta * scaleFactor;

    const rodBottom = bottomY + deformPx;

    const rodLength = rodBottom - topY;

    const rodWidth = 18;

    // 杆件颜色：根据应力状态变化

    const stressRatio = Math.min(Math.abs(currentDelta) / (deltaSt * 2 +
0.001), 1.0);

    const r = 40 + 180 * stressRatio;

    const gCol = 180 - 140 * stressRatio;

    const b = 200 - 170 * stressRatio;

    const rodColor = `rgb(${Math.min(r,255)}, ${Math.max(gCol,40)},
${Math.max(b,40)})`;

    ctx.save();

    // 杆件阴影

    ctx.shadowColor = 'rgba(0,0,0,0.06)';

    ctx.shadowBlur = 10;

    ctx.shadowOffsetX = 2;

    ctx.shadowOffsetY = 2;

```

```
// 杆件主体 (带渐变)

const grad = ctx.createLinearGradient(cx - rodWidth / 2, topY, cx +
rodWidth / 2, topY);

grad.addColorStop(0, '#5d6d7e');
grad.addColorStop(0.2, rodColor);
grad.addColorStop(0.8, rodColor);
grad.addColorStop(1, '#5d6d7e');
ctx.fillStyle = grad;

const rx = cx - rodWidth / 2;
const ry = topY;
const rw = rodWidth;
const rh = rodLength;
if (rh > 2) {
    ctx.fillRect(rx, ry, rw, rh);
}

ctx.shadowBlur = 0;
ctx.strokeStyle = '#2c3e50';
ctx.lineWidth = 1.2;
if (rh > 2) {
    ctx.strokeRect(rx, ry, rw, rh);
}

// 杆件上的刻度标记

if (Math.abs(currentDelta) > 0.0005) {
```

```

    ctx.strokeStyle = 'rgba(44,62,80,0.25)';

    ctx.lineWidth = 0.8;

    const numMarks = 6;

    for (let i = 1; i < numMarks; i++) {

        const t = i / numMarks;

        const yPos = topY + t * rodLength;

        const offset = 5 + 8 * (1 - Math.abs(currentDelta) / (deltaSt
* 2 + 0.001));

        ctx.beginPath();

        ctx.moveTo(cx - rodWidth / 2 - offset, yPos);

        ctx.lineTo(cx - rodWidth / 2 - 2, yPos);

        ctx.stroke();

        ctx.beginPath();

        ctx.moveTo(cx + rodWidth / 2 + offset, yPos);

        ctx.lineTo(cx + rodWidth / 2 + 2, yPos);

        ctx.stroke();

    }

}

ctx.restore();

```

// ---- 变形标注 ----

```

if (Math.abs(currentDelta) > 0.0001) {

    ctx.save();

    const sign = currentDelta >= 0 ? '+' : '-';

    const deltaDisplay = (currentDelta * 1000).toFixed(1);

    ctx.fillStyle = '#c0392b';

    ctx.font = 'bold 14px "Segoe UI", sans-serif';

```

```
ctx.textAlign = 'left';  
ctx.textBaseline = 'bottom';  
const labelX = cx + rodWidth / 2 + 14;  
const labelY = rodBottom - 4;  
ctx.fillText(`δ = ${sign}${\deltaDisplay} mm`, labelX, labelY);
```

```
// 变形箭头线
```

```
ctx.strokeStyle = 'rgba(192,57,43,0.35)';  
ctx.lineWidth = 1.4;  
ctx.setLineDash([4, 4]);  
const arrowX = cx + rodWidth / 2 + 52;  
ctx.beginPath();  
ctx.moveTo(arrowX, bottomY);  
ctx.lineTo(arrowX, rodBottom);  
ctx.stroke();  
ctx.setLineDash([]);
```

```
// 箭头头
```

```
if (Math.abs(currentDelta) > 0.0005) {  
    ctx.fillStyle = 'rgba(192,57,43,0.4)';  
    const dir = currentDelta >= 0 ? 1 : -1;  
    const tipY = rodBottom;  
    ctx.beginPath();  
    ctx.moveTo(arrowX, tipY);  
    ctx.lineTo(arrowX - 6, tipY - 8 * dir);  
    ctx.lineTo(arrowX + 6, tipY - 8 * dir);  
    ctx.closePath();  
    ctx.fill();  
}
```

```

    }

    ctx.restore();
}

// ---- 载荷箭头 (底部) ----

const loadY = rodBottom + 14;

ctx.save();

const loadColor = (mode === 'sudden' && currentDelta > deltaSt *
1.1) ? '#e74c3c' : '#d35400';

ctx.fillStyle = loadColor;

ctx.strokeStyle = loadColor;

ctx.lineWidth = 2.8;


// 箭头线

ctx.beginPath();

ctx.moveTo(cx, loadY);

ctx.lineTo(cx, loadY + 50);

ctx.stroke();


// 箭头头

ctx.beginPath();

ctx.moveTo(cx - 10, loadY + 40);

ctx.lineTo(cx, loadY + 50);

ctx.lineTo(cx + 10, loadY + 40);

ctx.closePath();

ctx.fill();

```

```

// 载荷标签

ctx.fillStyle = '#2c3e50';

ctx.font = 'bold 15px "Segoe UI", sans-serif';

ctx.textAlign = 'center';

ctx.textBaseline = 'top';

const label = mode === 'static' ? `P = ${P.toFixed(0)} N (静载)` : `P =
${P.toFixed(0)} N (突加)`;

ctx.fillText(label, cx, loadY + 56);


// 重物方块 (代表质量)

ctx.fillStyle = '#e67e22';

ctx.shadowColor = 'rgba(0,0,0,0.1)';

ctx.shadowBlur = 8;

const blockSize = 28;

const bx = cx - blockSize / 2;

const by = loadY - 8 - blockSize;

ctx.fillRect(bx, by, blockSize, blockSize);

ctx.shadowBlur = 0;

ctx.strokeStyle = '#7f3f00';

ctx.lineWidth = 1.2;

ctx.strokeRect(bx, by, blockSize, blockSize);

ctx.fillStyle = 'fff';

ctx.font = 'bold 12px "Segoe UI", sans-serif';

ctx.textAlign = 'center';

ctx.textBaseline = 'middle';

ctx.fillText('m', cx, by + blockSize / 2);

ctx.restore();

```

```

// ---- 工况标签 ----

ctx.save();

ctx.fillStyle = '#2c3e50';

ctx.font = 'bold 16px "Segoe UI", sans-serif';

ctx.textAlign = 'left';

ctx.textBaseline = 'top';

const modeLabel = mode === 'static' ? '🏠 静载荷工况' : '💣 突加
载荷工况';

ctx.fillText(modeLabel, 24, 22);

// 显示动荷系数

const Kd = mode === 'sudden' ? 2.0 : 1.0;

ctx.fillStyle = '#27ae60';

ctx.font = 'bold 15px "Segoe UI", sans-serif';

ctx.textAlign = 'right';

ctx.textBaseline = 'top';

ctx.fillText(`K_d = ${Kd.toFixed(3)}`, W - 24, 22);

// 显示当前变形与最大变形

ctx.fillStyle = '#6b7f93';

ctx.font = '13px "Segoe UI", sans-serif';

ctx.textAlign = 'right';

ctx.textBaseline = 'top';

const deltaCur = (currentDelta * 1000).toFixed(1);

const deltaMaxDisp = (maxDelta * 1000).toFixed(1);

```

```
        ctx.fillText(`当前变形: ${deltaCur} mm | 最大变形: ${deltaMaxDisp} mm`, W - 24, 44);
```

```
    ctx.restore();
```

```
    // ---- 图例 ----
```

```
    ctx.save();
```

```
    const legX = 24,
```

```
          legY = 74;
```

```
    ctx.font = '12px "Segoe UI", sans-serif';
```

```
    ctx.textAlign = 'left';
```

```
    ctx.textBaseline = 'top';
```

```
    ctx.fillStyle = '#6b7f93';
```

```
    ctx.fillText('■ 杆件 (刚度 k)', legX, legY);
```

```
    ctx.fillStyle = '#d35400';
```

```
    ctx.fillText('■ 载荷 P', legX + 140, legY);
```

```
    ctx.fillStyle = '#c0392b';
```

```
    ctx.fillText('↓ 变形  $\delta$ ', legX + 240, legY);
```

```
    ctx.fillStyle = '#27ae60';
```

```
    ctx.fillText(`⚡  $K_d = \{K_d.toFixed(2)}\}$ ', legX + 340, legY);
```

```
    ctx.restore();
```

```
    // ---- 静载参考线 (显示静变形位置) ----
```

```
    if (mode === 'sudden' && deltaSt > 0.0001) {
```

```
        ctx.save();
```

```

        const stY = bottomY + deltaSt * scaleFactor;

        ctx.setLineDash([3, 5]);

        ctx.strokeStyle = 'rgba(39,174,96,0.5)';

        ctx.lineWidth = 1.4;

        ctx.beginPath();

        ctx.moveTo(cx - 44, stY);

        ctx.lineTo(cx + 44, stY);

        ctx.stroke();

        ctx.setLineDash([]);

        ctx.fillStyle = 'rgba(39,174,96,0.6)';

        ctx.font = '11px "Segoe UI", sans-serif';

        ctx.textAlign = 'left';

        ctx.textBaseline = 'bottom';

        ctx.fillText('δ_st', cx + 48, stY - 2);

        ctx.restore();

    }

}

```

// ----- 动画更新 -----

```

function updateAnimation(dt) {

    if (resetRequested) {

        resetRequested = false;

        time = 0;

        delta = 0;

        deltaMax = 0;

        if (mode === 'static') {

            delta = deltaSt;

```

```

        deltaMax = deltaSt;
    }

    return;
}

const dtClamped = Math.min(dt, 0.025);

if (mode === 'static') {
    // 静载：稳定在静变形

    delta = deltaSt;

    deltaMax = deltaSt;

    return;
}

// ---- 突加载荷 ----

const m = P / g;

const omegaVal = Math.sqrt(k / m);

const omegaD = omegaVal * Math.sqrt(1 - zeta * zeta);

// 解析解：  $\delta(t) = \delta_{st} * (1 - e^{(-\zeta\omega t)} * (\cos(\omega_d * t) + \zeta / \sqrt{1 - \zeta^2} * \sin(\omega_d * t)))$ 

// 当  $\zeta=0$  时：  $\delta(t) = \delta_{st} * (1 - \cos(\omega * t))$ 

let deltaT;

if (zeta < 0.001) {
    deltaT = deltaSt * (1 - Math.cos(omegaVal * time));
} else {
    const expTerm = Math.exp(-zeta * omegaVal * time);

```

```

        const cosTerm = Math.cos(omegaD * time);
        const sinTerm = Math.sin(omegaD * time);
        const factor = zeta / Math.sqrt(1 - zeta * zeta);
        deltaT = deltaSt * (1 - expTerm * (cosTerm + factor * sinTerm));
    }

    // 确保非负
    if (deltaT < 0) deltaT = 0;
    delta = deltaT;

    // 更新最大变形
    if (delta > deltaMax) {
        deltaMax = delta;
    }

    // 如果变形趋近于静变形且振荡幅度很小，认为稳定
    // 但不自动停止，让用户观察

    // 时间推进
    time += dtClamped;
}

// ----- 动画循环 -----

let lastTime = 0;
let frameCount = 0;

function animate(timestamp) {

```

```

    if (!lastTime) lastTime = timestamp;

    const dt = Math.min((timestamp - lastTime) / 1000, 0.05);

    lastTime = timestamp;

    // 更新物理

    updateAnimation(dt);

    // 绘制

    const currentMax = (mode === 'sudden') ? Math.max(deltaMax,
deltaSt) : deltaSt;

    drawScene(delta, currentMax, mode);

    // 更新状态显示

    const Kd = mode === 'sudden' ? 2.0 : 1.0;

    const deltaD = mode === 'sudden' ? 2 * deltaSt : deltaSt;

    const sigmaD = mode === 'sudden' ? 2 * sigmaSt : sigmaSt;

    infoDeltaD.textContent = (deltaD * 1000).toFixed(2) + ' mm';

    infoSigmaD.textContent = (sigmaD / 1e6).toFixed(2) + ' MPa';

    infoKd.textContent = Kd.toFixed(3);

    formulaKdVal.textContent = Kd.toFixed(3);

    formulaSigmaVal.textContent = (sigmaD / 1e6).toFixed(2) + ' MPa';

    animId = requestAnimationFrame(animate);
}

// ----- 切换工况 -----

function setMode(newMode) {

```

```
if (newMode === mode && mode !== 'static') {  
    // 如果相同模式，复位重新开始  
}  
  
mode = newMode;  
  
time = 0;  
  
delta = 0;  
  
deltaMax = 0;  
  
  
// 更新按钮状态  
  
btnStatic.classList.toggle('active', mode === 'static');  
  
btnSudden.classList.toggle('active', mode === 'sudden');  
  
  
// 更新模式标签  
  
modeStatus.textContent = mode === 'static' ? '静载荷' : '突加载荷';  
  
statusDetail.textContent = mode === 'static' ?  
    '杆件在静载作用下稳定变形':  
    '载荷突加，杆件产生振动，最大变形为静变形的 2 倍';  
  
  
// 更新物理计算  
  
computePhysics();  
  
updateDisplay();  
  
  
if (mode === 'static') {  
    delta = deltaSt;  
    deltaMax = deltaSt;  
} else {  
    // 突加载荷从 0 开始
```

```

        delta = 0;

        deltaMax = 0;
    }
}

// ----- 复位 -----

function resetAnimation() {
    resetRequested = true;

    time = 0;

    delta = 0;

    deltaMax = 0;

    if (mode === 'static') {
        delta = deltaSt;

        deltaMax = deltaSt;
    }

    computePhysics();

    updateDisplay();

    statusDetail.textContent = mode === 'static' ?

        '杆件在静载作用下稳定变形' :

        '载荷突加，杆件产生振动，最大变形为静变形的 2 倍';
}

// ----- 滑块更新 -----

function updateParams() {
    P = parseFloat(sliderP.value);

    k = parseFloat(sliderK.value);

    zeta = parseFloat(sliderZeta.value);

```

```
    valP.textContent = P.toFixed(0);

    valK.textContent = k.toFixed(0);

    valZeta.textContent = zeta.toFixed(2);


    computePhysics();

    updateDisplay();


    if (mode === 'static') {

        delta = deltaSt;

        deltaMax = deltaSt;

    } else {

        // 突加载荷：重置动画以应用新参数

        time = 0;

        delta = 0;

        deltaMax = 0;

    }

}


// ----- 事件绑定 -----

sliderP.addEventListener('input', updateParams);

sliderK.addEventListener('input', updateParams);

sliderZeta.addEventListener('input', updateParams);


btnStatic.addEventListener('click', function() {

    setMode('static');

});
```

```

btnSudden.addEventListener('click', function() {
    setMode('sudden');
});

btnReset.addEventListener('click', resetAnimation);

// ----- 窗口 resize -----

let resizeTimer;

window.addEventListener('resize', function() {
    clearTimeout(resizeTimer);
    resizeTimer = setTimeout(() => {
        drawScene(delta, (mode === 'sudden') ? Math.max(deltaMax,
deltaSt) : deltaSt, mode);
    }, 150);
});

// ----- 初始化 -----

computePhysics();

updateDisplay();

setMode('static');

// 启动动画

animId = requestAnimationFrame(animate);

console.log('✅ 静载荷 vs 突加载荷演示已启动');

console.log(`P=${P}N, k=${k}N/m, ζ=${zeta}, δ
_st=${(deltaSt*1000).toFixed(2)}mm`);

```

```
console.log('突加载荷动荷系数  $K_d = 2$  (恒成立)');
```

```
// 暴露全局变量用于调试
```

```
window.demo = {  
    setMode,  
    resetAnimation,  
    updateParams,  
    P: () => P,  
    k: () => k,  
    deltaSt: () => deltaSt  
};
```

```
})();
```

```
</script>
```

```
</body>
```

```
</html>
```